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Vectors (AS)

- J1 Use vectors in two dimensions.
- J2 Calculate the magnitude and direction of a vector and convert between component form and magnitude/direction form.
- J3 Add vectors diagrammatically and perform the algebraic operations of vector addition and multiplication by scalars, and understand their geometrical interpretations.
- J4 Understand and use position vectors; calculate the distance between two points represented by position vectors.
- J5 Use vectors to solve problems in pure mathematics and in context, including forces.

For a brief commentary on this content go to the <u>MEI outline SoW</u>.

Pre-requisites

- GCSE: Pythagoras' Theorem to be able to calculate distances between points and magnitudes of vectors.
- Trigonometry to be able to convert between different forms in which vectors can be expressed.

Common student errors

- Taking insufficient care with notation, such as writing 5 rather than 5i.
- Confusing position vectors with displacement vectors.
- Failing to sketch the vector, particularly when the context involves bearings.
- Making sign errors when calculating the magnitude of vectors with negative components.

Teaching it!

- A series of three <u>videos</u> designed to support students on this topic.
- <u>Properties of vectors</u>: Arranging a set of vectors so that each property is satisfied (<u>Solution</u>).
- <u>Vector addition and subtraction</u>: A useful GeoGebra file for introducing this topic.
- <u>Hit the spot</u>: An interactive challenge from Underground Mathematics involving combining vectors.
- <u>Grid moves</u>: A very simple intro to vectors from Don Steward for use with struggling students.
- Introduction to vectors (student task): <u>Autograph</u>, <u>GeoGebra</u>

Getting them thinking

- Change one component of $\mathbf{a} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$, $\mathbf{b} = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$, $\mathbf{c} = \begin{pmatrix} 4 \\ 3 \end{pmatrix}$ so that $\mathbf{a} + \mathbf{b}$ is parallel to \mathbf{c} .
- Give me an example of a vector with magnitude 5...now give me an unusual example.
- Prove that the medians of any triangle are concurrent.
- Varignon's Theorem states that for any quadrilateral, the midpoints of the sides form the vertices of a parallelogram. Prove this using vectors.